

## Oxford Revise | Edexcel A Level Maths | Answers

- Method (M) marks are awarded for showing you know a method and have attempted to apply it.
- Accuracy (A) marks should only be awarded if the relevant M marks have been awarded.
- Unconditional accuracy (B) marks are awarded independently of M marks. They do not rely on method.
- The abbreviation **o.e.** means 'or equivalent (and appropriate)'.

## Please note that:

- efficient use of advanced calculators is expected
- inexact numerical answers should be given to three significant figures unless the question states otherwise; values from statistical tables should be quoted in full
- when a value of g is required, it is taken as  $g = 9.8 \,\mathrm{m\,s^{-2}}$  unless stated otherwise in the question.

## **Chapter 2 Quadratics and their graphs**

| Question | Answer                                                                | Extra information     | Marks   |
|----------|-----------------------------------------------------------------------|-----------------------|---------|
|          | $x^2 - 2x + 6 = (x - 1)^2 + 5$                                        | Completing the square | M1      |
| 2.1      | Since square numbers are always $\geq 0$ , the expression will always |                       |         |
|          | be greater than or equal to 5, which is greater than 0                | Correct conclusion    | A1      |
|          | Total                                                                 |                       | 2 marks |
| 2.2 (a)  | $2x^2 + 20x + 17 = 2(x^2 + 10x) + 17$                                 | Correct factorisation | M1      |
|          | $= 2[(x+5)^2 - 25] + 17$<br>= 2(x+5)^2 - 33                           | Completing the square | M1      |
|          | $=2(x+5)^2-33$                                                        | Simplifying           | A1      |
| 2.2 (b)  | -33                                                                   | Correct minimum       | B1      |



| Question | Answer                                                                                         | Extra information                                           | Marks   |
|----------|------------------------------------------------------------------------------------------------|-------------------------------------------------------------|---------|
| 2.2 (c)  | -5                                                                                             | Correct value                                               | B1      |
|          | Total                                                                                          |                                                             | 5 marks |
|          | Since the <i>x</i> -intercepts are 1 and 3, the equation will be of the form $y = a(x-1)(x-3)$ | Use of general equation                                     | M1      |
| 2.2      | The <i>y</i> -intercept of this equation will be at $a \times (-1) \times (-3) = 3a$           | Correct equation for constant term                          | M1      |
| 2.3      | Since the <i>y</i> -intercept is at 9, this means that $a = 3$                                 | Correct a value                                             | M1      |
|          | The equation of the curve is therefore $y = 3(x - 1)(x - 3)$ , which expands to                |                                                             | A 1     |
|          | $y = 3x^2 - 12x + 9$                                                                           | Correct equation                                            | A1      |
|          | Total                                                                                          |                                                             | 4 marks |
| 2.4 (a)  | (a-5)(a-1) = 0<br>a = 5 or $a = 1$                                                             | Attempting to solve. Can be implied from correct solutions. | M1      |
|          | a = 5  or  a = 1                                                                               | Correct solutions                                           | A1      |
| 2.4 (b)  | $a = \sqrt{b}$                                                                                 | Correct substitution                                        | M1      |
|          | $b = a^2$ , therefore $b = 5^2 = 25$ or $b = 1^2 = 1$                                          | Use of their results from (a)                               | A1      |
|          | Total                                                                                          |                                                             | 4 marks |



| Question | Answer                                                     | Extra information                                 | Marks   |
|----------|------------------------------------------------------------|---------------------------------------------------|---------|
|          | One example where it is either true or false. For example: | One example showing claim is either true or false | M1A1    |
|          | If $x = 5$ , $(5-5)^2 + 10 = 10$ ; $4 \times 5 = 20$       |                                                   |         |
|          | 10 is not greater than 20, so the statement is false.      |                                                   |         |
| 2.5      | One example where it is the opposite. For example:         | Second example to show opposite result            | A1      |
|          | If $x = 12$ , $(12-5)^2 + 10 = 49$ ; $4 \times 12 = 48$    |                                                   |         |
|          | 59 is greater than 48, so the statement is true.           |                                                   |         |
|          | The student's claim is sometimes true.                     | Correct conclusion                                | A1      |
|          | Total                                                      |                                                   | 4 marks |
|          | $\sqrt{p}(3-81p\sqrt{p})$ Since $p \neq 0$                 | Any correct first step                            | M1      |
|          |                                                            |                                                   |         |
|          | $3 - 81p\sqrt{p} = 0$                                      | Statement that expression inside brackets = 0     | M1      |
|          | $3 = 81p\sqrt{p}$ $1 = 27p\sqrt{p}$                        |                                                   |         |
| 2.6 (a)  | $1 = 27 p \sqrt{p}$                                        |                                                   |         |
|          | $p^{\frac{3}{2}} = \frac{1}{27}$                           |                                                   |         |
|          | $p^3 = \frac{1}{729}$                                      |                                                   |         |
|          | $p = \frac{1}{9}$                                          | Correct solution                                  | A1      |



| Question | Answer                                               | Extra information                            | Marks   |
|----------|------------------------------------------------------|----------------------------------------------|---------|
|          | $x^4 - 20x^2 + 64 = (x^2)^2 - 20(x^2) + 640$         | Identifying quadratic in $x^2$               | M1      |
| 26(b)    | $(x^2 - 4)(x^2 - 16) = 0$<br>$x^2 = 4$ or $x^2 = 16$ |                                              |         |
| 2.0 (0)  | $x^2 = 4$ or $x^2 = 16$                              | Correct values for $x^2$                     | M1      |
|          | x = 2, -2, 4  or  -4                                 | All four solutions                           | A1      |
|          | Total                                                |                                              | 6 marks |
|          | $2\sin^2\theta + \sin\theta - 1 = 0$                 | Identification of quadratic in $\sin \theta$ | M1      |
|          | $(2\sin\theta - 1)(\sin\theta + 1) = 0$              |                                              |         |
| 2.7      | $\sin \theta = \frac{1}{2}$ or $\sin \theta = -1$    | Correct values for $\sin \theta$             | M1      |
|          | $\theta = 30^{\circ},  \theta = -90^{\circ}$         | Both solutions correct                       | A1      |
|          | Total                                                |                                              | 3 marks |
| 2.8 (a)  | £350                                                 | Maximum point correctly identified           | B1      |
| 2.8 (b)  | x-8=0                                                |                                              |         |
| 2.8 (0)  | £8                                                   | Correct value                                | B1      |
| 2.8 (c)  | $P = 350 - 14(15 - 8)^2$                             | Correct substitution                         | M1      |
|          | =-£336                                               |                                              |         |
|          | They would make a loss of £336                       | Correct conclusion                           | A1      |



| Question | Answer                                                                                                                                                                                                                              | Extra information                  | Marks   |
|----------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------|---------|
|          | $350 - 14(x - 8)^2 = 200$                                                                                                                                                                                                           | Correct substitution               | M1      |
| 20(4)    | $x - 8 = \pm 3.27$                                                                                                                                                                                                                  | Sight of $\pm 3.27$                | M1      |
| 2.8 (d)  | x = 11.27 or $x = 4.73$                                                                                                                                                                                                             | Both solutions, to at least 3 s.f. | M1      |
|          | £5                                                                                                                                                                                                                                  | Correct conclusion                 | A1      |
|          | Total                                                                                                                                                                                                                               |                                    | 8 marks |
|          | $4x^3 - 37x^2 + 9x = 0$                                                                                                                                                                                                             | Rearranging                        | M1      |
|          | $x(4x^2 - 37x + 9) = 0$                                                                                                                                                                                                             | One factor found                   | M1      |
| 2.9 (a)  | x(4x-1)(x-9) = 0                                                                                                                                                                                                                    | Fully factorising                  | M1      |
|          | $x(4x^{2} - 37x + 9) = 0$ $x(4x - 1)(x - 9) = 0$ $x = 0, x = \frac{1}{4}, x = 9$                                                                                                                                                    | All three correct solutions        | A1      |
|          | $x = (y+3)^2$                                                                                                                                                                                                                       | Identifying substitution           | M1      |
|          | $(y+3)^2 = 0 \implies y = -3$                                                                                                                                                                                                       | Correct solution                   | A1      |
| 2.9 (b)  | $x = (y+3)^{2}$ $(y+3)^{2} = 0 \implies y = -3$ $(y+3)^{2} = \frac{1}{4} \implies y+3 = \pm \frac{1}{2} \implies y = -2.5 \text{ or } y = -3.5$ $(y+3)^{2} = 9 \implies y+3 = \pm 3 \implies y = 0 \text{ or } y = -6$ <b>Total</b> | Both solutions for second equation | A1      |
|          | $(y+3)^2 = 9 \implies y+3 = \pm 3 \implies y = 0 \text{ or } y = -6$                                                                                                                                                                | Both solutions for third equation  | A1      |
|          | Total                                                                                                                                                                                                                               |                                    | 8 marks |



| Question | Answer                                                                                                | Extra information                                                                       | Marks   |
|----------|-------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------|---------|
|          | $(-2)^2 - 4 \times 1 \times (k+1) = 0$                                                                | Use of $b^2 - 4ac = 0$ seen or implied                                                  | M1      |
|          | 4 - 4(k+1) = 0                                                                                        |                                                                                         |         |
| 2.10     | 4 = 4(k+1)                                                                                            |                                                                                         |         |
| 2.10     | 1 = k + 1                                                                                             |                                                                                         |         |
|          | k = 0                                                                                                 |                                                                                         |         |
|          | So having exactly one real root implies that $k = 0$                                                  | Correct solution                                                                        | A1      |
|          | Total                                                                                                 |                                                                                         | 2 marks |
|          | The <i>x</i> -intercepts are 20 and 140, so the equation will be of the form $J = a(x - 20)(x - 140)$ | Expressing as general quadratic. Both <i>x</i> -intercepts must be identified for mark. | M1      |
|          | The graph is symmetrical, so the maximum point will be at $x = 80$                                    | Use of symmetrical property                                                             | M1      |
|          | When $x = 80$ , $y = 360$ , which is the maximum number of jackets sold.                              | Coordinates of turning point identified                                                 | M1      |
| 2.11     | Substituting $x = 80$ into the equation and setting it equal to 360 gives:                            | Use of the constant term to find the value of a                                         | M1      |
|          | 360 = a(80 - 20)(80 - 140)                                                                            |                                                                                         |         |
|          | 360 = a(60)(-60)                                                                                      |                                                                                         |         |
|          | $a = 360 \div -3600 = -0.1$                                                                           |                                                                                         |         |
|          | The equation of the curve is therefore $J = -\frac{1}{10}(x-20)(x-140)$                               |                                                                                         |         |
|          | which, in the required form, expands to $J = -\frac{1}{10}x^2 + 16x - 280$                            | Correct equation in correct form                                                        | A1      |
|          | Total                                                                                                 |                                                                                         | 5 marks |



| Question | Answer                                     | Extra information                     | Marks   |
|----------|--------------------------------------------|---------------------------------------|---------|
|          | $-2x^2 + 12x - k = -2(x^2 - 6x) - k$       | Correct first step                    | M1      |
| 2.12 (a) | $=-2[(x-3)^2-9]-k$                         | Completing the square                 | M1      |
|          | $= -2(x-3)^2 + (18-k)$                     | Simplifying                           | A1      |
| 2.12 (b) | 18-k                                       | Correct maximum                       | B1      |
|          | When $x = -4$ , $y = 0$                    | Correct method using either intercept | M1      |
|          | $0 = -2 \times (-4)^2 + 12 \times -4 - k$  |                                       |         |
|          | $0 = -2 \times 16 - 48 - k$                |                                       |         |
|          | k = -32 - 48                               |                                       |         |
|          | k = -80                                    | Correct value of <i>k</i>             | A1      |
| 2.12 (c) | or                                         |                                       |         |
|          | When $x = 10$                              |                                       |         |
|          | $y = -2 \times (10)^2 + 12 \times -10 - k$ |                                       |         |
|          | $y = -2 \times 100 + 12 \times 10 - k$     |                                       |         |
|          | k = -200 + 120                             |                                       |         |
|          | k = -80                                    |                                       |         |
|          | Total                                      |                                       | 6 marks |
|          | $2 \times 2^{2x} - 9 \times 2^x + 4 = 0$   | Identifying quadratic in $2^x$        | M1      |
|          | $(2 \times 2^x - 1)(2^x - 4) = 0$          |                                       |         |
| 2.13     | $2^x = \frac{1}{2}$ or $2^x = 4$           | For both solutions of the quadratic   | M1      |
|          | x = -1 or $x = 2$                          | Both solutions correct                | A1      |
|          | Total                                      |                                       | 3 marks |



| Question | Answer                                                         | Extra information                                                             | Marks   |
|----------|----------------------------------------------------------------|-------------------------------------------------------------------------------|---------|
|          | To have one repeated root $b^2 - 4ac = 0$                      | Statement of rule                                                             | B1      |
|          | $(-5k)^2 - 4 \times 1 \times (9k + 7) = 0$                     | Correct method                                                                | M1      |
|          | $25k^2 - 36k - 28 = 0$                                         |                                                                               |         |
|          | Using the quadratic equation:                                  |                                                                               |         |
|          | $k = \frac{36 \pm \sqrt{1296 - 4 \times 25 \times (-28)}}{50}$ | Any attempt to solve quadratic. Can be implied by sight of correct solutions. | M1      |
| 2.14 (a) | $=\frac{36\pm\sqrt{4096}}{}$                                   |                                                                               |         |
|          | =                                                              |                                                                               |         |
|          | $=\frac{36\pm64}{}$                                            |                                                                               |         |
|          | 50                                                             |                                                                               |         |
|          | or by factorising:                                             |                                                                               |         |
|          | (25k + 14)(k - 2) = 0                                          |                                                                               |         |
|          | k = 2 is the only valid solution                               | Correct conclusion                                                            | A1      |
|          | When $k = 2$                                                   | Substituting their value for <i>k</i> from (a)                                | M1      |
|          | $f(x) = x^2 - 10x + 25$                                        |                                                                               |         |
| 2.14 (b) | $x^2 - 10x + 25 = 0$                                           | Identification of perfect square. Can be implied by correct final             | M1      |
|          | $(x-5)^2=0$                                                    | answer.                                                                       |         |
|          | x = 5                                                          | Correct solution                                                              | A1      |
|          | Total                                                          |                                                                               | 7 marks |



| Question | Answer                                                                     | Extra information                   | Marks   |
|----------|----------------------------------------------------------------------------|-------------------------------------|---------|
|          | When $n$ is even, $n = 2k$                                                 | Correct proof for all even <i>n</i> | M1      |
|          | $n^3 + 6 = (2k)^3 + 6$                                                     |                                     |         |
|          | $=8k^3+6$                                                                  |                                     |         |
|          | which is not divisible by 8                                                |                                     |         |
|          | When $n$ is odd, $n = 2k + 1$                                              | Correct proof for all odd <i>n</i>  | M1      |
| 2.15     |                                                                            |                                     |         |
|          | $=8k^3+12k^2+6k+1+6$                                                       |                                     |         |
|          | $=2(4k^3+6k^2+3k+3)+1$                                                     |                                     |         |
|          | Odd numbers are not divisible by 8 as all multiples of 8 are               | Valid reasoning                     | M1      |
|          | even.                                                                      |                                     |         |
|          | Therefore, $n^3 + 6$ is never divisible by 8, for all $n \in \mathbb{N}$   | Correct conclusion                  | A1      |
|          | Total                                                                      |                                     | 4 marks |
| 2.16     | $42^2 - 42 + 41 = 1763$ , which is $41 \times 43$ and therefore not prime. | Any valid counter example           | B1      |
|          | Total                                                                      |                                     | 1 mark  |