

Oxford Revise | Edexcel A Level Maths | Answers

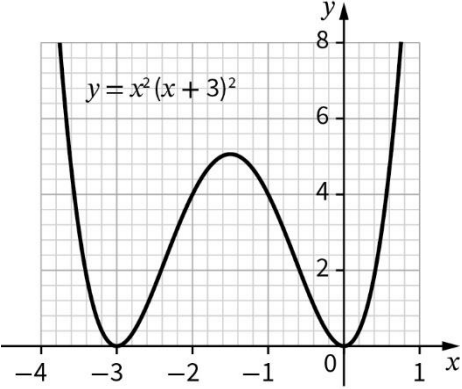
- Method (**M**) marks are awarded for showing you know a method and have attempted to apply it.
- Accuracy (**A**) marks should only be awarded if the relevant M marks have been awarded.
- Unconditional accuracy (**B**) marks are awarded independently of M marks. They do not rely on method.
- The abbreviation **o.e.** means 'or equivalent (and appropriate)'.

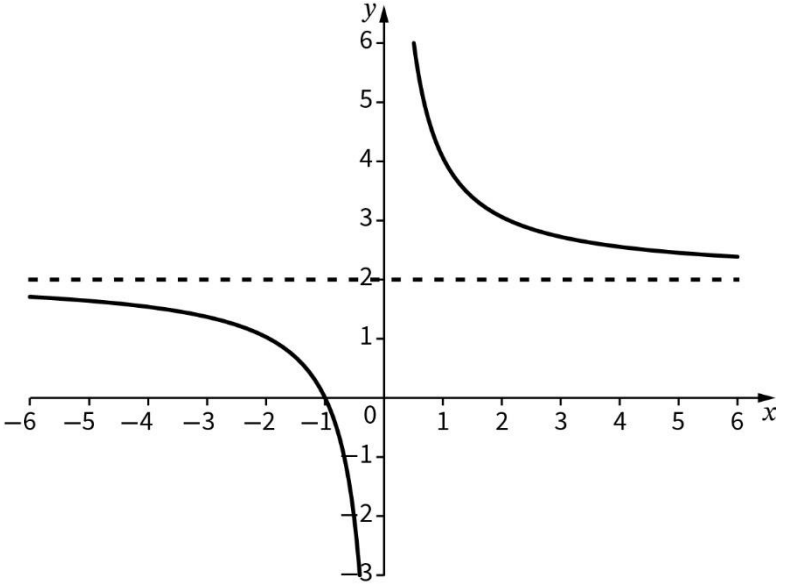
Please note that:

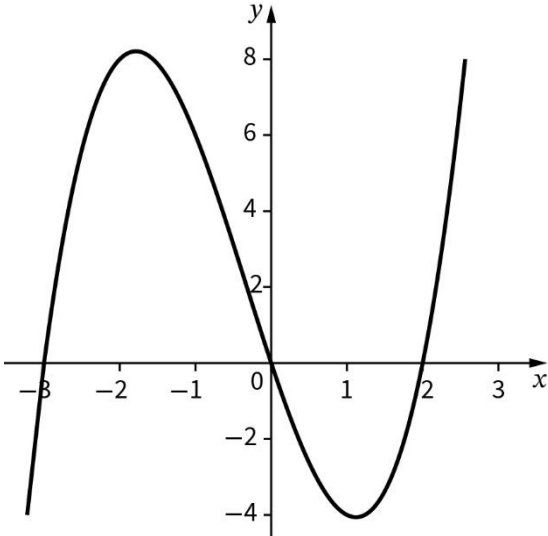
- efficient use of advanced calculators is expected
- inexact numerical answers should be given to three significant figures unless the question states otherwise; values from statistical tables should be quoted in full
- when a value of g is required, it is taken as $g = 9.8 \text{ m s}^{-2}$ unless stated otherwise in the question.

Chapter 6 Graphs of functions

Question	Answer	Extra information	Marks
6.1	<p>$y = x(x + 1)(x - 2)$</p>	<p>Correct shape of curve</p> <p>Correct x-intercepts</p>	<p>B1</p> <p>B1</p>
	Total		2 marks

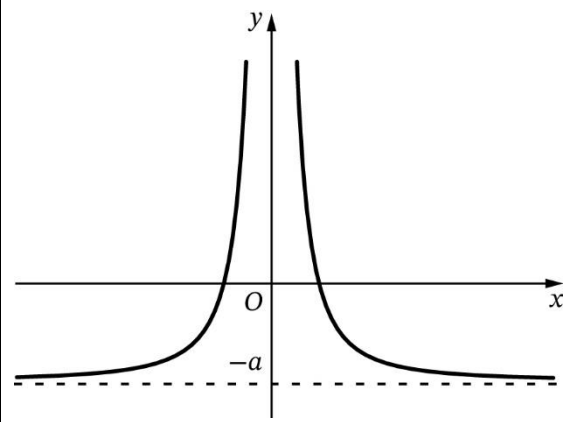
Question	Answer	Extra information	Marks
6.2		<p>Correct shape of curve</p> <p>Correct x-intercepts</p>	<p>B1</p> <p>B1</p>
	Total		2 marks
6.3 (a)	$0 = \frac{k}{x} + 2$ $-2 = \frac{k}{x} \Rightarrow x = -\frac{k}{2}, y = 0$	<p>Setting $y = 0$</p> <p>Solving to find x in terms of k</p>	<p>M1</p> <p>A1</p>

Question	Answer	Extra information	Marks
6.3 (b)	 <p>$y = 2$</p>	<p>Correct shape of curve. Must have both branches.</p> <p>Horizontal asymptote shown</p> <p>Equation of asymptote</p>	<p>B1</p> <p>B1</p> <p>B1</p>
	Total		5 marks
6.4 (a)	$f(x) = x(x^2 + x - 6)$ $f(x) = x(x + 3)(x - 2)$	<p>Taking out x as a factor</p> <p>Fully correct factorisation</p>	<p>M1</p> <p>A1</p>
6.4 (b)	$x(x + 3)(x - 2) = 0$ $x = 0, x = -3, x = 2$	<p>All three solutions correct</p>	<p>B1</p>

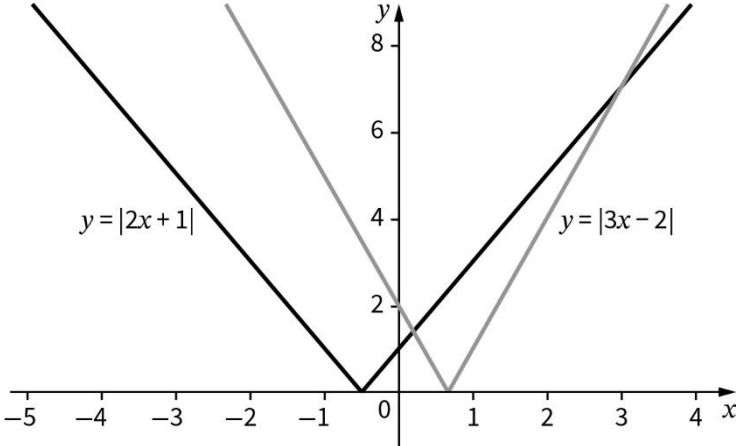
Question	Answer	Extra information	Marks
6.4 (c)		<p>Correct shape of curve</p> <p>Correct x-intercepts at -3 and 2</p>	<p>B1</p> <p>B1</p>
6.4 (d)	$x^3 + x^2 - 6x = 9 + 3x$ $x^3 + x^2 - 6x - 9 - 3x = 0$ $x^2(x+1) - 9(x+1) = 0$ $(x^2 - 9)(x+1) = 0$ $(x+3)(x-3)(x+1) = 0$ $x = -3, y = 0 \Rightarrow (-3, 0)$ $x = 3, y = 18 \Rightarrow (3, 18)$ $x = -1, y = 6 \Rightarrow (-1, 6)$	<p>Correctly equating expressions and moving terms to one side</p> <p>Fully factorising the expression</p> <p>Solving for x and finding the corresponding y-coordinates</p>	<p>M1</p> <p>M1</p> <p>A1</p>
	Total		8 marks

Question	Answer	Extra information	Marks
6.5	$y = x$ and $2y - x = 6$	Attempting to solve 'positive' version of the modulus function	M1
	$2y - y = 6$	Finding one variable	M1
	$y = 6$	Both coordinates correct	A1
	When $y = 6, x = 6$, so the point is $(6, 6)$		
6.5	$y = -x$ and $2y - x = 6$	Attempting to solve 'negative' version of the modulus function	M1
	$2y + y = 6$	Finding one variable	M1
	$3y = 6$	Both coordinates correct	A1
	$y = 2$		
	When $y = 2, x = -2$, so the point is $(-2, 2)$		
	Total		6 marks
6.6	Because the graph does not pass through the origin	Correct explanation	B1
	Total		1 mark
6.7	Because the area of a circle is a multiple of the square of its radius, not of its radius	Correct explanation	B1
	Total		1 mark

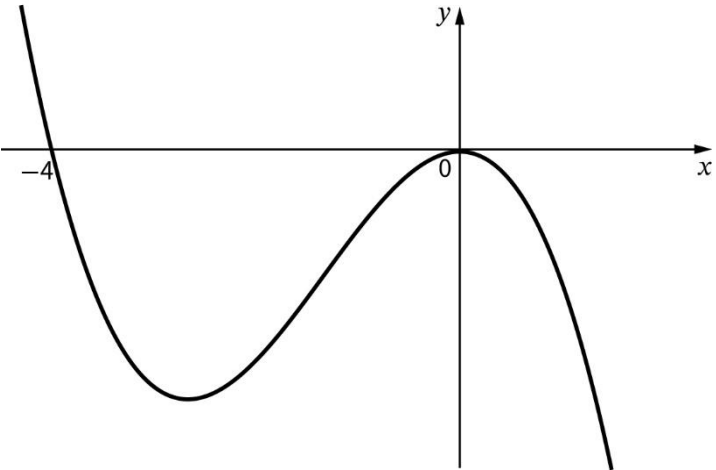
Question	Answer	Extra information	Marks
6.8 (a)		<p>For single curve with correct shape</p> <p>For the curve approaching both positive axes as asymptotes</p>	<p>B1</p> <p>B1</p>
6.8 (b)	$F = \frac{k}{d^2}$ $\frac{k}{(0.95d)^2} = \frac{1}{0.95^2} \times \frac{k}{d^2}$ $= 1.108033... \times \frac{k}{d^2}, \text{ so an increase of } 10.8\%$	<p>Correct format for this type of proportionality</p> <p>Attempting to calculate the increase</p> <p>Correct interpretation of the calculation</p>	<p>M1</p> <p>M1</p> <p>A1</p>
	Total		5 marks
6.9 (a)	$a = kb$ $b = jc$ where j, k are constants $a = k(jc)$ $a = (jk)c$ j, k are constants, so jk is also constant Therefore, a is directly proportional to c	<p>Correct structure for direct proportion</p> <p>Substituting for b and correct conclusion</p>	<p>M1</p> <p>A1</p>

Question	Answer	Extra information	Marks
6.9 (b)	$8 = 2k$, so $k = 4$ $3 = 6j$, so $j = 0.5$ Therefore, $a = 4 \times 0.5 \times c$ So, $c = 0.5a$	Correctly substituting $a = 8$, $b = 2$ to find k Correctly substituting $b = 3$, $c = 6$ to find j Correct formula	M1 M1 A1
6.9 (c)	$5 = 0.5a$ $a = 10$	Correct value for a	B1
	Total		6 marks
6.10 (a)	 <p>$y = -a$</p>	Correct shape curve. Must have both branches. Horizontal asymptote shown, where $a > 0$ Equation of asymptote	B1 B1 B1

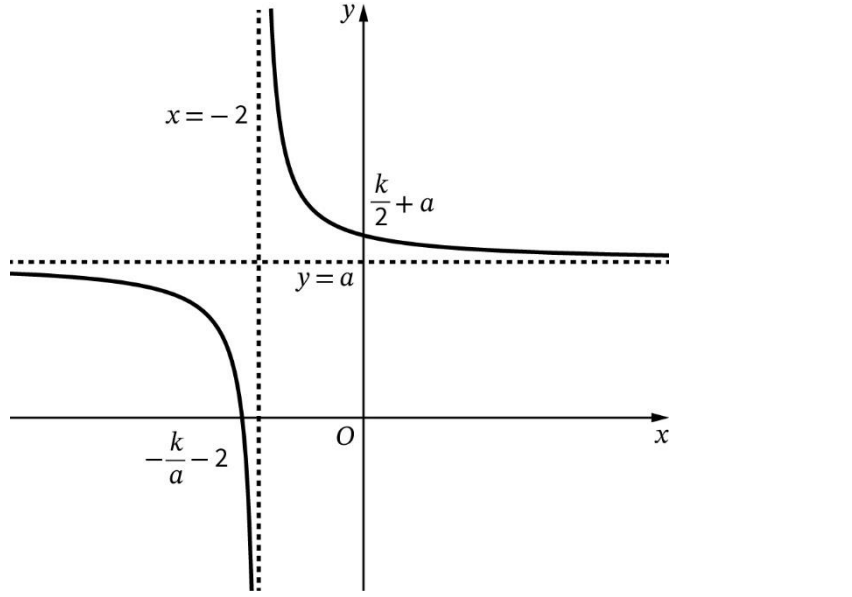
Question	Answer	Extra information	Marks
6.10 (b)	$0 = \frac{k}{x^2} - a$ $x^2 = \frac{k}{a} \Rightarrow x = \pm \sqrt{\frac{k}{a}}$ $\left(\sqrt{\frac{k}{a}}, 0\right) \text{ and } \left(-\sqrt{\frac{k}{a}}, 0\right)$	Setting $y = 0$ Correct positive x value Correct negative x value	M1 A1 A1
6.10 (c)	$\left(\sqrt{\frac{8}{2}}, 0\right) \text{ and } \left(-\sqrt{\frac{8}{2}}, 0\right)$ $x = 2 \text{ or } x = -2$	Substituting $k = 8$ and $a = 2$ into expression from (b) Both values correct	M1 A1
	Total		8 marks

Question	Answer	Extra information	Marks
6.11 (a)	 <p>Points of intersection:</p> <p>$f(x)$ meets the x-axis at $-\frac{1}{2}$, and $g(x)$ meets the x-axis at $\frac{2}{3}$</p> <p>$f(x)$ meets the y-axis at 1, and $g(x)$ meets the y-axis at 2</p>	<p>$f(x) = 2x + 1$ correct shape with point in the correct quadrant</p> <p>$g(x) = 3x - 2$ correct shape with point in the correct quadrant</p> <p>Two correct x-intercepts</p> <p>Two correct y-intercepts</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p>

Question	Answer	Extra information	Marks
6.11 (b)	<u>Point 1</u> $2x + 1 = 3x - 2$ $x = 3$ When $x = 3$, $y = 7$, so the point is (3, 7)	For right-hand intersection point where both graphs are 'positive' Correct coordinates	M1 A1
	<u>Point 2</u> $2x + 1 = -(3x - 2)$ $2x + 1 = -3x + 2$ $5x = 1$ $x = 0.2$ When $x = 0.2$, $y = 1.4$, so the point is (0.2, 1.4)	For left-hand intersection point where the first graph is 'positive' and the second graph is 'negative' Correct coordinates	M1 A1
6.11 (c)	$0.2 < x < 3$	Correct range	B1
	Total		9 marks

Question	Answer	Extra information	Marks
6.12 (a)		<p>Correct shape of curve</p> <p>Correct x-intercepts at -4 and 0</p>	<p>B1</p> <p>B1</p>
6.12 (b)	$-x^2(x + 4) = -x$ $x - 4x^2 - x^3 = 0$ $-x(x^2 + 4x - 1) = 0$ $b^2 - 4ac = 16 - (-4)$ $= 20 > 0$ <p>The quadratic has two solutions and so the cubic has three solutions and the graph $y = f(x)$ will intersect $y = -x$ three times.</p>	<p>Correct first step</p> <p>For forming cubic equal to 0</p> <p>For use of discriminant</p> <p>Correct conclusion</p>	<p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p>
	Total		6 marks
6.13 (a)	$(4, -1)$	One mark per correct coordinate	B1B1

Question	Answer	Extra information	Marks
6.13 (b)	$2(x - 4) - 1 = x - 2$ $2x - 8 - 1 = x - 2$ $x = 7$ $-2(x - 4) - 1 = x - 2$ $-2x + 8 - 1 = x - 2$ $3x = 9$, therefore $x = 3$	For 'positive' intersection Correct solution For 'negative' intersection Correct solution	M1 A1 M1 A1
6.13 (c)	$2 x - 4 < x - 1 \rightarrow 2 x - 4 - 1 < x - 2$ $\{x: 3 < x < 7\}$	Recognising that this is the same inequality Correct range of values	M1 A1
6.13 (d)	When the line touches the vertex of the graph $y = k - x$ passes through $(4, -1)$ $-1 = k - 4$ $k = 3$ The line will intersect the graph more than once when $k > 3$	Correct substitution Correct range	M1 A1
	Total		10 marks

Question	Answer	Extra information	Marks
6.14 (a)		<p>Correct shape curve with two branches</p> <p>Asymptote drawn and labelled at $x = -2$</p> <p>Asymptote drawn and labelled at $y = a$, where a is positive</p> <p>x-intercept labelled $-\frac{k}{a} - 2$</p> <p>y-intercept labelled $\frac{k}{2} + a$</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p>
6.14 (b)	$0 = \frac{k}{-2.6+2} + a \quad \text{and} \quad 6.5 = \frac{k}{0+2} + a$ $0.6a = k$ $13 - 2a = k$ $a = 5 \quad \text{and} \quad k = 3$	<p>For both substitutions</p> <p>Two simplified equations in a and k</p> <p>Solving simultaneously to find both values</p>	<p>M1</p> <p>M1</p> <p>A1</p>
	Total		8 marks

Question	Answer	Extra information	Marks
6.15 (a)	Identifying either $(x + 1)$ or $(x - 1)$ as a factor $x^3 - x = x(x^2 - 1)$ $= x(x + 1)(x - 1)$	Finding the first factor Fully factorising the expression	M1 A1
6.15 (b)	$\frac{5x+1}{x^3-x} = \frac{A}{x} + \frac{B}{x+1} + \frac{C}{x-1}$ $5x+1 = A(x+1)(x-1) + Bx(x-1) + Cx(x+1)$ $A = -1, B = -2, C = 3$ $-\frac{1}{x} - \frac{2}{x+1} + \frac{3}{x-1}$	Correct structure and method One variable correct Fully correct partial fractions	M1 A1 A1
	Total		5 marks

